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# Transport properties of liquid argon in krypton nanochannels: Anisotropy and non-homogeneity introduced by the solid walls

F. Sofos, T. Karakasidis \*, A. Liakopoulos

Hydromechanics and Environmental Engineering Laboratory, School of Engineering, University of Thessaly, 38834 Pedion Areos, Volos, Greece

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#### ABSTRACT

In this work we calculate the transport properties of liquid argon flowing through a nanochannel formed by krypton walls. Non-equilibrium molecular dynamics (NEMD) simulations are performed assuming flow conditions corresponding to the macroscopic equivalent of planar Poiseuille flow. We examine the effect of channel width and system temperature on diffusion coefficient, shear viscosity and thermal conductivity. The results show clearly the existence of a critical width, in the range  $7-18\sigma$ , below which the behavior of transport properties is affected in comparison to bulk properties. In fact for small width values, diffusion coefficient is highly anisotropic, the component normal to the wall being the smaller one. For the same width range, diffusivities along all directions are higher in the central layers than those close to the walls. Similarly, shear viscosity increases for small channel width values while thermal conductivity decreases. All properties approach bulk values as the channel width increases. The layers close to the walls always present distinctly different behavior due to the interaction with the wall atoms. The observed behavior is of particular importance in the design of nanofluidic devices.

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# 1. Introduction

Micro and nanofluidic simulations have attracted considerable attention recently, due to the growing interest for nanosystems in many technological and scientific fields. Experimental studies at the atomic scale are difficult to perform and, thus, atomistic simulation techniques provide the means for exploring regions (either in physical space or in parameter space) that cannot be accessed by experiment. Consequently, molecular computer simulations have established themselves as a valuable alternative to theoretical and experimental work. In addition to its role in interpreting experimental results, molecular computer simulation is vital in determining physical properties of materials as well as in exploratory research [1].

Among computer simulation techniques, equilibrium molecular dynamics (EMD) has been extensively used for the calculation of transport properties of fluids in equilibrium. For atomic systems far from equilibrium, such as liquid flows in channels, non-equilibrium molecular dynamics (NEMD) offers an effective flow simulation method as well as an alternative method for the calculation of transport properties of liquids, either in simple monoatomic fluids [2–9] or in more complex fluids [10–12]. Among the transport properties, diffusion coefficient, shear viscosity and thermal conductivity have attracted most of the interest of the scientific

community as they control the rates of mass, momentum and energy transport.

Diffusivity issues concerning liquid flows at nanoscale have been addressed by many researchers. Bitsanis et al. [13] studied fluid argon both in equilibrium and in Couette flow and concluded that diffusivity is not affected by the presence of flow in the system. Murad et al. [14] studied confined fluids in slit, tubular and cubic pores and found that diffusion coefficient values are not systematically affected by the size of the channels studied for channel width, h, in the range  $h=6\sigma-10\sigma$ , where  $\sigma$  is the LJ-potential length scale. A useful review on diffusivity issues in slit pores in [3] shows that mobility is maintained even in pore widths of  $2.0\sigma$ , while diffusion parallel to the pore wall below  $h=4.0\sigma$  becomes an oscillating function of the channel width. Beyond  $4.0\sigma$ , diffusivity increases smoothly and it reaches the bulk value at  $11.57\sigma$ .

Shear viscosity is another transport property of fluids that has attracted considerable interest among researchers. A number of computational studies of shear viscosity by EMD or NEMD have been reported in the literature. In the area of nanofluidics, Bitsanis et al. [15] found that shear viscosity in Poiseuille flow is indistinguishable from the homogenous fluid viscosity down to channel widths of  $6-7\sigma$ , while, below  $4\sigma$ , viscosity vs. channel width becomes an oscillating function. Hu et al. [16] found that the viscosity of a confined lubricant increases as the channel width decreases.

EMD or NEMD calculation of thermal conductivity in nanochannels is of particular interest, too. Evans [17], in his early work on thermal conductivity of argon in a confined system, found that this

<sup>\*</sup> Corresponding author. Tel.: +30 2421074163; fax: +30 2421074169. E-mail address: thkarak@uth.gr (T. Karakasidis).

Nome	nclature		
L <sub>x</sub> L <sub>y</sub> L <sub>z</sub> h V T N	Length of the computational domain in the $x$ -direction Length of the computational domain in the $y$ -direction Length of the computational domain in the $z$ -direction Channel width Volume of the computational domain $(L_x \times L_y \times L_z)$ Temperature Number of atoms	$egin{aligned} MSD \ v^i \ u(\mathbf{r}_{ij}) \ \mathbf{J}_{\mathbf{p}} \ \mathbf{J}_{\mathbf{q}} \ \mathbf{v}_i \ \mathbf{I} \end{aligned}$	Mean square displacement <i>i</i> th component of atomic velocity, <i>i</i> = 1,2,3 LJ potential of atom <i>i</i> with atom <i>j</i> Microscopic stress tensor Microscopic heat flow Velocity vector of atom <i>i</i> Unitary tensor
$K$ $\mathbf{r}_i$ $\mathbf{r}_{ij}$ $\mathbf{r}_{eq}$ $F_{ext}$ $k_B$ $m$ $D$ $D_{lay}$	Spring constant Position vector of atom $i$ Distance vector between $i$ th and $j$ th atom Position of a wall atom on fcc lattice site External driving force (magnitude) Boltzman constant Argon atom mass Diffusion coefficient, $D = \frac{D_x + D_y + D_z}{3}$ Diffusion coefficient value in a specific layer along the channel	Greek s $\sigma$ $\varepsilon$ $\rho^*$ $\eta_s$	symbols  Length parameter in the LJ potential Energy parameter in the LJ potential Reduced density Shear viscosity Thermal conductivity

quantity is linearly dependent to the external field applied to drive the flow. Murad et al. [18] showed that the vertical to the walls component of thermal conductivity is affected by the value of the elastic spring constant of the channel walls; its value decreases as this constant increases. Liu et al. [19] calculated thermal conductivity for thin argon films with Fourier's law and found that thermal conductivity increases as the film thickness increases, until it reaches the bulk value at 100 nm. Yonetani and Kinugawa [20] compared calculated values on thermal conductivity with experimental measurements of liquid para-hydrogen and found that it increases as temperature rises.

In nanochannels of width below  $6\sigma$ , the above transport properties have not been thoroughly studied with NEMD as far as we know. Wall-fluid interactions play a crucial role in the behavior of flow properties in channels of small width, especially in the range  $h = 2.65\sigma - 18.58\sigma$  [21]. The no-slip condition at the wall and the parabolic behavior of the velocity profile, expected from the continuum theory, break down in channels of small width and density profiles reveal strong ordering of the fluid. Thus, it is expected that the calculation of transport properties in small confined systems, especially at layers adjacent to the walls, will be of interest both from the fundamental point of view as well as for technological applications such as MEMS, lab-on-chip applications, nanomixers, etc.

When the width of the channel becomes very small, wall roughness becomes important. Roughness at the atomic scale can be classified as thermal, random or periodic [22]. Several molecular dynamics simulation works [22–27] examine mainly the effect of the roughness on the slip length. The results for simple fluids indicate that surface roughness can lead to slip near the solid boundary and affect fluid ordering [23–25]. For more complex fluids (water, hexadecane) the general trend observed is that the diffusion coefficient decreases near a rough wall [26] and viscosity is increased [27]. In our work we have assumed atomically flat wall surfaces so that only thermal roughness affects our transport property results.

In this work we study the transport properties of liquid argon by non-equilibrium molecular dynamics (NEMD) simulation of Poiseuille flow between two "infinite" krypton walls. We report on calculated values of the diffusion coefficient, D, shear viscosity,  $\eta_s$  and thermal conductivity,  $\lambda$ , for channel widths in the range  $2.65\sigma$ – $18.58\sigma$  and system temperature from 100 to 150 K. All transport properties are calculated both in distinct layers parallel to the channel walls as well as average values over the whole computational domain.

This paper is organized as follows. In Section 2 the molecular system modeled is described. The basis for the calculation of three transport properties  $(D, \eta_s, \lambda)$  is briefly presented in Section 3. Results are shown and discussed in Section 4, and concluding remarks are presented in Section 5.

## 2. System modeling

The NEMD technique is used to simulate planar Poiseuille flow of liquid argon. The geometry of the system under examination is presented schematically in Fig. 1. The walls consist of two layers of krypton atoms arranged on fcc lattice. Atomic interactions are described by a Lennard–Jones 12–6 potential:

$$v^{\mathrm{LJ}}(r_{ii}) = 4\varepsilon ((\sigma/r_{ii})^{12} - (\sigma/r_{ii})^{6}) \tag{1}$$

where the parameters of the Lennard–Jones potential are:  $\sigma_{\text{Ar}-\text{Ar}} = 0.3405 \text{ nm}$ ,  $\sigma_{\text{Kr}-\text{Kr}} = 0.3633 \text{ nm}$ ,  $\sigma_{\text{Ar}-\text{Kr}} = 0.3519 \text{ nm}$ ,  $\varepsilon_{\text{Ar}-\text{Ar}}/k_{\text{B}} = 119.8 \text{ K}$ ,  $\varepsilon_{\text{Kr}-\text{Kr}}/k_{\text{B}} = 167.0 \text{ K}$ ,  $\varepsilon_{\text{Ar}-\text{Kr}}/k_{\text{B}} = 141.4 \text{ K}$ , the cut-off radius is  $r_{\text{c}} = 2.5\sigma$ , the atomic mass of argon is  $m_{\text{Ar}} = 39.95$  a.u. and the atomic mass of krypton is  $m_{\text{Kr}} = 83.8$  a.u.

Flows in several nanochannels of variable width (h) have been simulated (see Table 1). The average fluid density  $\rho^*$  = 0.642 (in units of  $\sigma^{-3}$ ) has been kept constant. The streamwise and spanwise dimensions  $L_x$  and  $L_y$  as well as the number of wall atoms are kept constant throughout this work ( $L_x = L_y = 36.15$  Å,  $N_{\rm Kr} = 288$ ). Periodic boundary conditions are assumed in the x- and y-direction.

Wall atoms are kept around their original fcc lattice positions due to an elastic spring potential  $u_{\text{wall}}(\mid \mathbf{r}(t) - \mathbf{r}_{\text{eq}} \mid) = \frac{1}{2}K \mid \mathbf{r}(t) - \mathbf{r}_{\text{eq}} \mid)^2$ , where  $\mathbf{r}(t)$  is the position of an atom at time t,  $\mathbf{r}_{\text{eq}}$  is its initial lattice position and K is the spring constant. As explained in [28], if we compute the second derivative of this potential and the second derivative of the LJ potential (Eq. (1)), evaluate

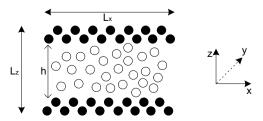


Fig. 1. The atomic system under examination.

**Table 1**Dimensions of the systems under examination

Case	$L_z$ (Å)	h (Å)	h/σ	Fluid atoms
1	18.08	9.04	2.65	192
2	24.10	15.06	4.42	320
3	36.15	27.11	7.9	576
4	72.30	63.26	18.58	1344

both derivatives at  $r = r_0 = 2^{1/6}\sigma$ , and equate the results, we get  $K = 57.15\varepsilon/\sigma^2$ . We remind the reader that  $r_0 = 2^{1/6}\sigma$  is the distance where the LJ potential reaches its minimum. The value of  $K = 57.15\varepsilon/\sigma^2$  was used in all our simulations.

An external driving force  $F_{\rm ext}$  is applied along the x direction to every fluid particle during the simulation. The magnitude of the external applied force is selected in order to avoid non-linear variations in fluid temperature induced by the flow [4] and is equal to 1.8075 pN. The wall atoms absorb the increase in kinetic energy of the fluid atoms and Nosé–Hoover thermostats at the thermal walls are employed in order to keep the system's temperature constant. A detailed description of the use of Nosé–Hoover thermostats is provided in references [29] and [30]. We use two independent thermostats one for the upper wall and another for the lower wall in order to achieve better thermalisation of the wall atoms.

The simulation step is  $10^{-2}$  ps. In the beginning of a simulation run fluid atoms are located on fcc sites. Atoms are assigned appropriate random initial velocities in order to reach the desired temperature. The system reaches equilibrium state after a run of  $10^5$  timesteps (NVE). Then, NEMD simulations are performed with a duration of  $10^5$  timesteps.

# 3. Theoretical relations

The diffusion coefficient can be obtained using either the Einstein's relation

$$D = \lim_{t \to \infty} \frac{1}{2dNt} \left\langle \sum_{j=1}^{N} [\mathbf{r}_j (t) - \mathbf{r}_j(0)]^2 \right\rangle$$
 (2)

or Green-Kubo's relation

$$D = \frac{1}{3N} \int_0^\infty \left\langle \sum_{i=1}^N \mathbf{v}_j(0) \cdot \mathbf{v}_j(t) \right\rangle$$
 (3)

where  $\mathbf{r}_j$  is the position vector of the jth atom and d is the dimensionality of the system (d = 1 for diffusivity calculation in one direction, d = 2 in two directions and d = 3 in three directions) and  $\mathbf{v}_j$  is the velocity vector of the jth atom.

The two relations are equivalent and provide the same results [2,3]. Relations 2 and 3 are derived for systems in equilibrium, but they can be used for non-equilibrium systems as well, provided one excludes the drift contribution from the flow [3]. In the present work we have used Einstein's relation for the calculation of the diffusion coefficient. The computation is carried out in two steps. In the first step the Mean Square Displacement (MSD) is obtained from the definition

$$MSD(t) = \frac{1}{N} \left\langle \sum_{i=1}^{N} [\mathbf{r}_{j}(t) - \mathbf{r}_{j}(0)]^{2} \right\rangle$$
 (4)

and subsequently D is evaluated based on Eq. (2) which can be written as

$$D = \lim_{t \to \infty} \frac{1}{2dt} MSD(t) \tag{5}$$

Shear viscosity and thermal conductivity for systems in equilibrium can be calculated using the Green–Kubo formalism, as described in

[31]. These relations can be used without modification in NEMD as long as we stay in the linear regime close to equilibrium [32]. When the system is not in equilibrium, due to the existence of an external force, the magnitude of the external force should be small enough for linearization to hold [4,33]. Our system is in the linear regime for all channel widths studied when  $F_{\text{ext}} = 1.8075 \text{ pN}$ .

Shear viscosity  $\eta_s$  for a pure fluid is computed by the relation

$$\eta_{\rm s} = \frac{1}{Vk_{\rm R}T} \int_0^\infty {\rm d}t \langle J_{\rm p}^{xy}(t) \cdot J_{\rm p}^{xy}(0) \rangle \tag{6}$$

where  $J_{\rm p}^{\rm xy}$  is the off-diagonal component of the microscopic stress tensor

$$J_{p}^{xy} = \sum_{i=1}^{N} m_{i} v_{i}^{x} v_{i}^{y} - \sum_{i=1}^{N} \sum_{j>1}^{N} r_{ij}^{x} \frac{\partial u(r_{ij})}{\partial r_{ij}^{y}}$$
 (7)

 $u(r_{ij})$  is the LJ potential of atom i interacting with atom j,  $r_{ij}$  is the distance between atoms i and j, and  $v_i^j$  is the j-component (j = x, y or z) of the velocity of atom i.

On the other hand, thermal conductivity  $\lambda$  can be calculated by the integration of the time-autocorrelation function of the elements of the microscopic heat flow  $J_{\alpha}^{x}$ , i.e.,

$$\lambda = \frac{1}{V k_{\rm B} T^2} \int_0^\infty \mathrm{d}t \langle J_{\rm q}^x(t) \cdot J_{\rm q}^x(0) \rangle \tag{8}$$

where the microscopic heat flow  $J_a$  is given by

$$\mathbf{J}_{\mathbf{q}} = \frac{1}{2} \sum_{i=1}^{N} m_i (v_i)^2 v_i - \sum_{i=1}^{N} \sum_{i>1}^{N} \left[ \mathbf{r}_{ij} : \frac{\partial u(r_{ij})}{\partial \mathbf{r}_{ij}} - \mathbf{I} \cdot u(r_{ij}) \right] \cdot v_i$$
 (9)

where  $v_i$  is the velocity vector of atom i and I is the unitary matrix.

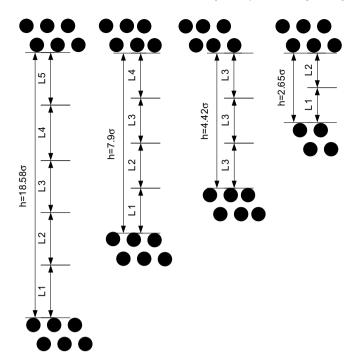
# 4. Results and discussion

All transport properties are computed both in distinct layers and as total average values for the channel. The number of layers used in the computation varies and depends on the width of the channel. Specifically, two layers are considered in the channel of width  $h = 2.65\sigma$ , three layers for  $h = 4.42\sigma$ , four layers for  $h = 7.9\sigma$  and five layers for  $h = 18.58\sigma$ , as shown in Fig. 2.

## 4.1. Diffusion coefficient

In Fig. 3a–c, we present the MSD diagrams in the streamwise direction (x-direction), the spanwise direction (y-direction) and the direction normal to the walls (z-direction) at 100, 120 and 150 K for h =  $2.65\sigma$  (MSD is presented in reduced units ( $MSD^*$ )). Diffusion coefficient values are extracted from MSD values according to Eq. (5). The diffusion coefficient in the z-direction has a rather small value and the Mean Square Displacement (MSD) diagram presents a small slope, meaning that fluid atoms are only slightly diffusing in the direction normal to the walls. The slope is significantly greater in the x- and y-directions.

Diffusion coefficient values were calculated for appropriately selected layers of equal width and the values are tabulated in Tables 2–5. At small channel widths ( $h \leq 15\sigma$ ) local diffusion coefficient values in the z-direction ( $D_{\text{lay},z}$ ) are smaller than those in the x- and y-directions ( $D_{\text{lay},x}$ ,  $D_{\text{lay},y}$ ), which are practically the same. This is attributed to the fact that fluid atoms are strongly confined due to presence of the solid boundaries and, in the long term their diffusivity in the z-direction ( $D_{\text{lay},z}$ ) approaches zero value [3]. On the contrary,  $D_{\text{lay},x}$  and  $D_{\text{lay},y}$  are larger since the mobility of the fluid atoms is not inhibited by solid walls in these directions. However, as channel width increases ( $h = 15\sigma$ ),  $D_{\text{lay},z}$  values approach  $D_{\text{lay},x}$  and  $D_{\text{lay},y}$  in all inner layers, except the two layers adjacent to the walls. This means that there is always strong anisotropy in



**Fig. 2.** Layer partitioning along each channel for the computation of transport properties.

diffusion coefficient in a layer of width about 1–1.5 $\sigma$  adjacent to the walls.

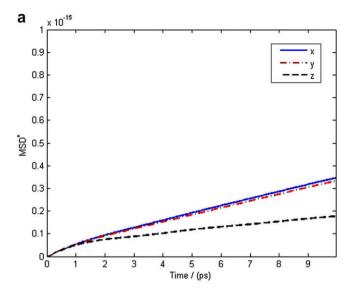
Comparing the values of the diffusion coefficient, we observe that all components of the diffusion coefficient are greater in the inner layers than they are at layers adjacent to the walls. This can be attributed to the fact that near the walls the repulsive solid/fluid effect is strong and fluid mobility in this region is small. At the inner layers, solid/fluid interaction is negligible, fluid atoms interact only with other identical fluid atoms (note that the fluid/fluid interaction potential is weaker than the solid/fluid) and their mobility is larger.

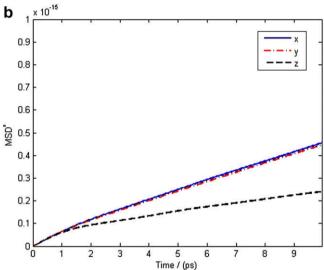
We also point out that the effect of system temperature is significant, since an increase in temperature from 100 to 120 K and, even more, to 150 K leads to a considerable rise in the respective diffusion coefficient values.

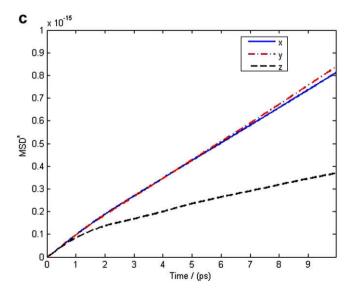
We turn now our attention back to the diffusion coefficient calculation based on the whole computational domain. It is of interest to summarize (Fig. 4) the calculated average channel diffusion coefficients  $D_x$ ,  $D_y$  and  $D_z$  for all channels at 100, 120 and 150 K. In Fig. 4a, we observe that diffusion is isotropic along the x- and y- directions. In contradistinction,  $D_z$  has a smaller value for  $h = 2.65\sigma$ , but increases with a greater slope as the channel width increases. All diffusion coefficients converge to bulk value [34] at  $h = 16\sigma$  and, furthermore, become isotropic. Similar behavior is observed for the other two system temperatures studied here (Fig. 4b and c). This behavior indicates the existence of a characteristic channel width ( $h \approx 15\sigma$ ) below which the diffusion behavior is anisotropic.

In Fig. 5 we summarize the calculated average total channel diffusivity  $D = \frac{D_x + D_y + D_z}{2}$  for all channels and temperatures studied. We can see that diffusivity is increasing as the channel width increases. One can explain the observed behavior if he takes into account the fact that at small channel widths the effect of walls on fluid atoms extends practically to the whole fluid range, resulting in an important modification of its behavior in comparison to the bulk where fluid atoms are embedded in the fluid environment. As the channel width increases, the percentage of fluid atoms that are out of the

wall interaction increases and, thus, we approach bulk-like behavior. A similar behavior has been observed in an early work of







**Fig. 3.** Mean Square Displacement diagrams (in reduced units), in x-, y- and z-directions for  $2.65\sigma$ -wide channel at (a) 100 K, (b) 120 K and (c) 150 K.

**Table 2** Layer diffusion coefficient values, at x-, y- and z-directions ( $D_{\text{lay},x}$ ,  $D_{\text{lay},y}$  and  $D_{\text{lay},z}$ , respectively), for a 2.65 $\sigma$ -wide channel at 100, 120 and 150 K and external driving force  $F_{\text{ext}}$  = 1.8075 pN

T/(K)	$10^5 \times D/$	$10^5 \times D/(\text{cm}^2/\text{s})$											
	$D_{\mathrm{lay},x}$		$D_{\mathrm{lay},y}$		$D_{\mathrm{lay},z}$								
	L1	L2	L1	L2	L1	L2							
100	1.53	1.54	1.57	1.58	0.58	0.60							
120	2.07	2.06	2.09	2.11	0.86	0.87							
150	4.05	4.05	3.87	4.02	1.37	1.37							

**Table 3** As in Table 3, but for  $4.42\sigma$ -wide channel

T/(K)	$10^5 \times 10^5$	$10^5 \times D/(\text{cm}^2/\text{s})$												
	$D_{\text{lay,x}}$			$D_{\text{lay},y}$			$D_{\mathrm{lay},z}$							
	L1	L2	L3	L1	L2	L3	L1	L2	L3					
100 120 150	1.59 2.47 3.89	2.93 3.86 5.40	1.61 2.43 3.77	1.56 2.44 3.83	3.06 3.93 5.45	1.57 2.49 3.85	1.18 1.68 2.58	1.92 2.43 3.21	1.16 1.68 2.60					

Sommers and Davis [34], in a model of Couette flow in smooth and structured pores.

The results clearly indicate that diffusivities of a liquid may differ significantly from their known bulk values for nanochannels below a given characteristic dimension. This behavior should be taken into account in the design of nanofluidic devices, as well as in interpreting particle nanovelocimetry (nanoPIV) measurements close to solid surfaces [35].

# 4.2. Shear viscosity

Fig. 6a and b show shear viscosity integral diagrams, based on Eq. (6) and their respective autocorrelation functions (ACFs) across a  $2.65\sigma$ -wide channel at 100, 120 and 150 K. The shear viscosity is calculated for layers L1 and L2, which are symmetrical with respect to the channel midplane. We present here results for layer L1 (computed values for L2 are the same within statistical errors). As we can see in Fig. 6a, the rise in temperature from 100 to 120 and 150 K results in a significant decrease in shear viscosity. The ACF diagram (see Fig. 6b) shows a fast decay to zero at 100 K right

after the beginning of the simulation, at t = 0.5 ps. At T = 120 and 150 K, the decay is also fast in the beginning, but a slightly slower decay follows and ACF goes to zero at t = 0.75 ps. Note that the fast decay to zero for each temperature studied is an additional evidence of linearity for our system [36].

In Fig. 7a and b, shear viscosity integrals and ACFs for a  $7.9\sigma$ -wide channel partitioned in four layers (L1–L4) at 120 K are presented. Shear viscosity is almost uniform across the channel and this fact reveals that solid/fluid interaction does not affect significantly the values of shear viscosity across the channel. ACFs in each channel layer converge to zero immediately after the beginning of the simulation. We obtain a similar uniform behavior for shear viscosity across the channel for h = 4.42 and  $18.58\sigma$  (at T = 100 and 150 K).

We summarize the total average shear viscosity values as a function of channel width and system temperature in Fig. 8. One can see that for all temperatures at small channel width we have large values of shear viscosity and its value decreases as the channel width increases to attain the bulk value above  $8\sigma$ . It can be seen that for higher system temperature the approach to bulk-like behavior is achieved faster. This behavior can be explained by the nature of shear viscosity which depends both on velocities and forces (Eqs. (6) and (7)). At small channel widths, the effect of different interactions of walls on fluid atoms extends nearly to the whole fluid and, as a result, we have an important modification of shear viscosity in comparison to bulk values. As the channel width increases, the percentage of fluid atoms that are out of the influence of wall increases resulting in a behavior close to the bulk. Increased temperature helps also overcome easier the effect of wall interactions. Thus, at higher temperature, approach to bulk-like behavior occurs faster.

It seems that the critical value of channel width in order to obtain bulk-like behavior for shear viscosity is similar to that in the case of diffusion coefficient, although it appears that is located rather at smaller values of h. The fact that shear viscosity is significantly larger compared to the bulk below a critical value is an important parameter that should be taken into consideration in the design of nanofluidic devices.

# 4.3. Thermal conductivity

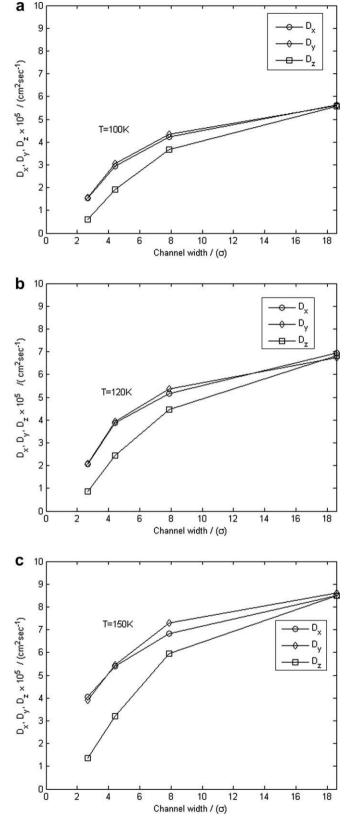
Fig. 9a and b show thermal conductivity integrals and ACF diagrams across a  $2.65\sigma$ -wide channel at 100, 120 and 150 K. Thermal conductivity is calculated for layers L1 and L2 (which are symmetrical with respect to the channel midplane). Here we present

**Table 4** As in Table 3, but for  $7.9\sigma$ -wide channel

T/(K)	$10^5 \times D/c$	$10^5 \times D/(\mathrm{cm}^2/\mathrm{s})$													
	$D_{\mathrm{lay},x}$				$D_{\mathrm{lay},y}$				$D_{lay,z}$						
	L1	L2	L3	L4	L1	L2	L3	L4	L1	L2	L3	L4			
100	2.31	4.19	4.24	2.27	2.21	4.31	4.33	2.17	1.80	3.62	3.68	1.77			
120	3.36	5.10	5.15	3.33	3.35	5.43	5.37	3.41	2.47	4.42	4.46	2.53			
150	4.91	6.83	6.86	4.94	5.03	7.29	7.04	4.88	3.53	5.95	5.90	3.42			

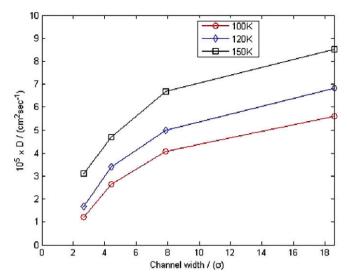
**Table 5** As in Table 3, but for  $18.58\sigma$ -wide channel

T/(K)	$10^5 \times D$	$10^5 \times D/(\text{cm}^2/\text{s})$													
	$D_{\mathrm{lay,x}}$					$D_{\text{lay},y}$	$D_{\mathrm{lay},y}$					$D_{lay,z}$			
	L1	L2	L3	L4	L5	L1	L2	L3	L4	L5	L1	L2	L3	L4	L5
100	4.00	5.68	5.62	5.49	3.80	3.90	5.65	5.59	5.75	3.85	3.24	5.56	5.56	5.46	3.26
120	5.22	6.74	6.93	6.70	5.21	5.07	6.92	6.74	6.73	4.98	4.11	6.68	6.82	6.55	4.10
150	6.63	8.16	8.50	8.40	6.88	6.69	8.58	8.71	8.49	6.80	5.19	8.14	8.54	8.21	5.23



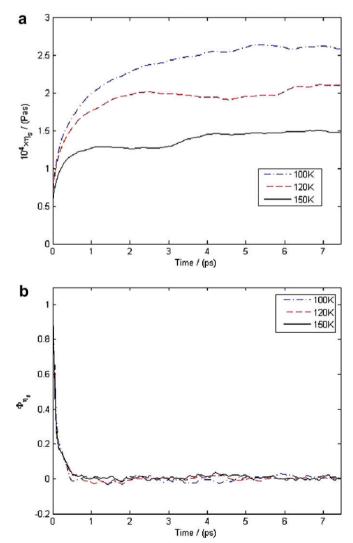
**Fig. 4.** Estimation of channel diffusion coefficient along the x-, y- and z-directions at (a) 100 K, (b) 120 K and (c) 150 K (lines are used only as a guide to the eye).

computed values for L1. It seems that as temperature rises from 100 to 120 and 150 K, thermal conductivity decreases slightly. The ACF diagrams decay to zero at t=1 ps at 120 and 150 K. At

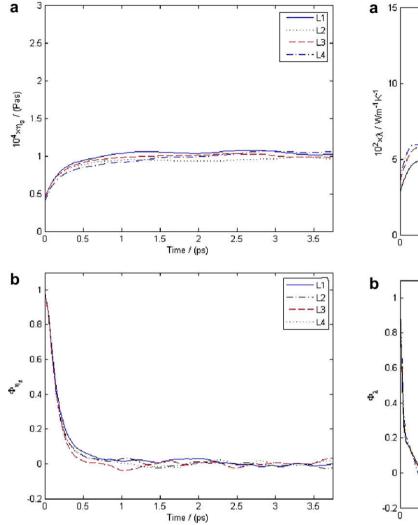


**Fig. 5.** Estimates of channel diffusion coefficient at 100, 120 and 150 K, for channel widths ranging from 2.65 to  $18.58\sigma$  (lines are used only as a guide to the eye).

100 K, apart from the fast convergence to zero, we observe a fall below zero at t = 0.5 ps before ACF stabilizes to zero.

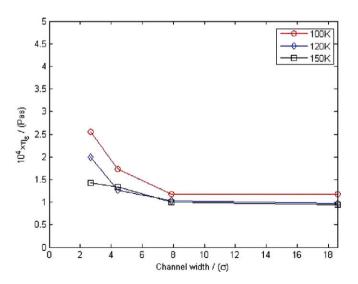


**Fig. 6.** Shear viscosity in layer L1 across a  $2.65\sigma$ -wide channel in (a) integral diagram (b) ACF diagram.

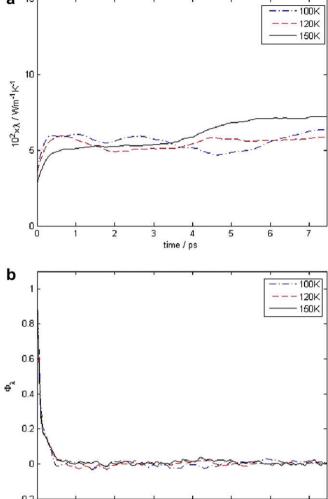


**Fig. 7.** Shear viscosity across a  $7.9\sigma$ -wide channel at 120 K in (a) integral diagrams (b) ACF diagrams. L1 and L4 layers are adjacent to the walls, L2 and L3 layers are in the midplane of the channel.

Thermal conductivity ACFs and integral diagrams calculated in four distinct layers (L1–L4) are shown in Fig. 11a and b. The chan-



**Fig. 8.** Estimation of shear viscosity at 100, 120 and 150 K, for channel widths ranging from 2.65 to  $18.58\sigma$  (lines are used only as a guide to the eye).



**Fig. 9.** Thermal conductivity in layer L1 across a  $2.65\sigma$ -wide channel in a) integral diagram b) ACF diagram.

Time / (ps)

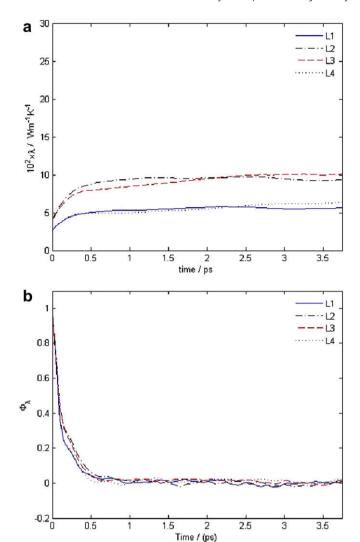
5

3

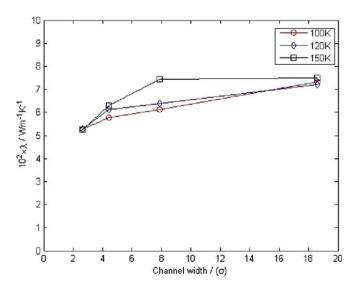
2

nel here is  $7.9\sigma$ -wide and the system temperature is 120 K. We observe that thermal conductivity is higher in the inner layers (L2, L3) compared to layers adjacent to the walls (L1, L4). All ACFs decay fast to zero as can be seen in Fig. 10b. We obtain a similar behavior for thermal conductivity across channels of width h = 4.42 and  $18.58\sigma$ .

The calculated average thermal conductivity coefficients versus channel width for all system temperatures studied are summarized in Fig. 11. We observe that for all temperatures at small channel widths we have small values of thermal conductivity while  $\lambda$  increases as the channel width increases to attain the bulk value at about  $h = 20\sigma$ . However, we observe that at higher temperature thermal conductivity reaches its bulk value at smaller channel widths. This behavior can be understood on physical grounds, since thermal conductivity depends both on velocities and forces (Eqs. (8) and (9)). For small channel widths, the effect of walls on fluid atoms extends to nearly the whole range of fluid. As a result, it modifies the fluid behavior in comparison to the bulk. As the channel width increases, the percentage of fluid that is out of range of the wall interaction increases and, as a result, the fluid approaches bulk-like behavior. Increased temperature helps also overcome earlier the effect of wall interactions, thus, at higher temperature we approach bulk-like behavior faster.



**Fig. 10.** Thermal conductivity across a 7.9 $\sigma$ -wide channel at 120 K in (a) integral diagrams (b) ACF diagrams. L1 and L4 layers are adjacent to the walls, L2 and L3 layers are in the midplane of the channel.



**Fig. 11.** Estimation of thermal conductivity at 100, 120 and 150 K, for channel widths ranging from 2.65 to  $18.58\sigma$  (lines are used only as a guide to the eye).

We believe that these effects (due primarily to the existence of the two solid/liquid interfaces) are important characteristics of flows in nanochannels and should be taken into account in the design of nanofluidic devices when heat transfer is significant.

We performed also simulations using three-layer fcc walls. In general, same results were obtained for diffusion coefficients and thermal conductivity. Shear viscosity, as a total average value for each channel, was not significantly affected by the number of wall atomic layers. However, in the case of three-layer walls, near the walls shear viscosity has smaller value (greater values near the channel centerline) compared to the values obtained for the two-layer walls.

# 5. Conclusions

We have presented a molecular dynamics study of planar Poiseuille nanoflow of liquid argon between krypton walls for channel widths, h, in the range  $2.65\sigma$ – $18.58\sigma$ .

Diffusivity is isotropic in planes parallel to the walls, i.e.,  $D_x$  and  $D_{v}$  are practically the same (x is the direction along the flow and y the spanwise direction, i.e., normal to flow direction and parallel to the walls). On the contrary, in the *z*-direction (normal to the walls) the diffusion coefficient  $D_z$  is significantly smaller than  $D_x$  and  $D_y$  in the narrow channels  $h = 2.65\sigma$  and  $h = 4.42\sigma$ . The ratio of  $D_z/D_x$  (or, similar ly,  $D_z/D_v$ ) increases as the channel width increases and reaches unity, i.e. isotropic diffusion for  $h = 18.58\sigma$ . The calculation of the diffusion coefficients in distinct layers parallel to walls reveal that diffusion is higher in layers close to the center of the channel and decreases for the layers adjacent to the walls. This behavior is attributed to the fact that these layers "feel" the presence of walls in contrast to the central layers that are surrounded only by fluid atoms and diffusion is not inhibited by the presence of the solid atoms. As the channel width increases bulk-like behavior is approached close to the centerline. The diffusion coefficient increases when the system temperature increases as the atomic mobility increases at elevated temperatures.

Shear viscosity values are affected by the channel width. The smaller the channel width the larger its value. However, for  $h \approx 8\sigma$ ,  $\eta_s$  attains its bulk value. Across the channel, shear viscosity profiles are nearly uniform with only a slight decrease near the walls. Shear viscosity is not significantly affected by the solid/fluid interaction. At 100 and 120 K thermal conductivity, as an average total value for the whole channel, increases slightly as channel width rises and reaches its bulk value at  $h = 20\sigma$ . At 150 K, thermal conductivity attains its bulk value for liquid argon at  $h \approx 8\sigma$  and retains it as h increases. Thermal conductivity calculated in layers, i.e., profiles across the channel reveal that the layers close to the channel centerline conduct the heat produced by the flow at a higher rate compared to the layers adjacent to the walls, i.e., thermal conductivity attains higher values as we approach the center of the channel.

The results show that transport properties exhibit a significantly different behavior than that of the bulk fluid below a critical channel width which in our system seems to be located in the region  $8-20\sigma$ . The existence of this critical width is attributed to the interaction of the fluid with the walls since at smaller channel widths the effect of the difference of interactions of the walls on the fluid extends practically to the whole range of the fluid modifying considerably its properties in comparison to the bulk. As the channel width increases there is an increasing percentage of fluid atoms that are located out of the wall range and, as a result, the fluid atoms attain bulk-like behavior. The size of the characteristic width may depend on the type of wall/fluid materials due to the different kind of atomistic interactions.

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